

# Finite Element Analysis

B.E. Sem. VIII [MECH/AUTO]

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## EVALUATION SYSTEM

	Time	Marks
<b>Theory Exam</b>	3 Hrs.	100
<b>Practical Exam</b>	–	–
<b>Oral Exam</b>	–	25
<b>Term Work</b>	–	25

## SYLLABUS

### 1. Introductory Concepts

Introduction to FEM. Brief History. General FEM procedure. Applications of FEM in various fields. Advantages and disadvantages of FEM.

Differential Equations in different fields: Types of Differential Equations. Primary and Secondary Variables and types of Boundary Conditions.

Matrix Algebra: Matrix operations, Gauss Elimination Method to get inverse of a Matrix. Partitioning of Matrix.

Numerical Integration: Trapezoidal rule, Simpson's  $1/3^{\text{rd}}$  rule, Newton Cotes formula, Gauss quadrature formula, Gauss quadrature in two dimensions.

### 2. Approximate solution of differential equations

Weighted residual techniques, collocation, Least squares and Galerkin methods.

**FEM Procedure :** Definitions of various terms used in FEM like element, order of the element, internal and external node/s, degree of freedom, primary and secondary variables, essential boundary conditions, natural boundary conditions, homogeneous and non-homogeneous boundary conditions.

### 3. Minimization of a functional

Principle of minimum total potential. Piecewise Rayleigh-Ritz method. Comparison with weighted residual method.

**Piecewise approximations:** Basis of Finite Element Methods. Formulation of matrix method--“stiffness matrix”; transformation and assembly concepts.

### 4. Example problems in one dimensional structural analysis, heat transfer and fluid flow (Stepped and Taper Bars, Fins, Fluid Network, Spring-Cart systems, Plane Trusses, Beams).

Elements of variational calculus. Band-width, aspect ratio, coarse and fine meshing, etc.

### 5. Two dimensional finite element formulations

Introduction, Three noded triangular element, four noded rectangular element, six noded triangular element, compatibility, four noded quadrilateral element, eight noded quadrilateral element, nine noded quadrilateral element.

**Natural coordinates and coordinate transformations:** Alternate methods for deriving shape functions, Natural coordinates – quadrilateral elements, Natural coordinates – triangular elements.

**Isoperimetric.** Algorithms for solution of equations. Convergence criterion, patch test and errors in finite element analysis. Method of Elimination. Sources of error

### 6. Finite element formulation of dynamics

Applications to free vibration problems. Lumped and consistent mass matrices. Algorithms for solution of Eigen value problems. Transient dynamics problems in heat transfer and solid mechanics.

**References Books :**

1. The Finite Element Method its Basis & Fundamentals (*O.C.Zienkiewicz, R.L.Taylor & J.Z.Zhu*) Butterworth-Heinemann, Elsevier
2. Finite Element Method, (*Reddy J. N.*) McGrawHill
3. The Finite Element Method in Engineering , 4th Edition (*S.S.Rao*) Academic Press, Elsevier
4. Finite Element Methods for Engineers (*U.S.Dixit*) Cengage Learning
5. Textbook of FE Analysis (*P.Seshu*) Prentice Hall
6. Introduction to Finite Elements Methods (*Desai and Abel*) CBS Publication.
7. Introduction to Finite Elements in Engineering (*Tirupati R. Chandrupatla & Ashok D.Belegundu*)
8. Introduction to Finite Element Methods (*Erik Thompson*) Wiley India.
9. Finite Elements Hand Book (*H. Kardestuneer*).
10. Concepts & Applications of Finite Element Analysis (*R.D.Cook*).
11. Finite Element Procedures in Engineering Analysis (*Bathe, K.J.*) Prentice Hall of India.
12. The Finite Element Method for Engineers (*Huebener K.H., Dewhirst D.D., Smith D.E. and Byrom T.G.*) John Wiley, New York.
13. Finite Element Methods (*Logan*) Cengage Learning
14. Finite Elements Analysis (*George Buchanan*) McGrawHill
15. Finite Elements Analysis (*C.S.Krishnamoorthy*) Tata McGrawHill
16. Concept and Application of Finite Element Methods (*Robert Cook*) Wiley India.

