

Ankit Pedwal,



Mahatma Gandhi Mission's College of Engineering and Technology
Kamothe, Navi Mumbai

APPLIED MATHEMATICS II

UNIT TEST II F.E.(All divisions) MAX MARKS 20 DURATION 50 min.

ANSWER ANY TWO QUESTIONS FROM Q1 and Q2.

Q1. (a) prove that $\beta(m+1, n) = \frac{m}{m+n} \beta(m, n)$ [04]

(b) Evaluate $\int_0^{\infty} e^{-\frac{x^4}{2}} dx$ [04] (c) Find perimeter of the curve $r = a(1 - \cos\theta)$ [04]

Q2 Prove that $\int_0^{\infty} \sqrt{y} e^{-y^2} dy \int_0^{\infty} \frac{e^{-y^2}}{\sqrt{y}} dy = \frac{\pi}{2\sqrt{2}}$ [06]

(b) Evaluate $\int_5^9 \sqrt{(9-x)(x-5)} dx$ [06]

(c) For the curve $y^2 = x(1-x/3)^2$ S.T $s^2 = y^2 + \frac{4}{3}x^2$ where s is the arc length measured from origin to any point (x, y) on it. [06]